## Exercise 11: Supporting an Arrow Debreu Equilibrium as a Sequence of Markets Equilibrium Edward C. Prescott March 7, 2002

There are i types with  $\lambda_i$  being the measure of type i. The Arrow-Debreu commodity point is  $\{x_t\}_{t=0,1,2,...}$  where  $x_t=(c_t,i_t,h_t,k_t)$ . Here  $c_t$  denotes date t consumption good,  $i_t$  date t investment good,  $h_t$  hours of date t labor services, and  $k_t$  is units of date t capital services. Let the allocation  $\{x^1,x^2,...,x^I,y\}$  and the price system  $\{p_t,q_t,w_t,r_t\}_{t=0,1,2,...}$  be an A-D competitive equilibrium. Here y is the aggregate commodity vector of the business sector. There are constant returns to scale. Only households own capital and supply capital services.

- i. Specify the credit-debt position per type i person as a function of the prices and x<sup>i</sup>.
- ii. For the sequence of market equilibrium that supports this allocation, specify the date t credit-debt position per type i person as a function of x<sup>i</sup> and the prices.